



MÄLARDALEN UNIVERSITY
SWEDEN

Operations planning and scheduling

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PPU426



Today's topic

- What is operations planning and scheduling?
- How to cope with mismatch between demand and supply?
- Production planning
- Scheduling
- Job shop scheduling theories

Production planning and scheduling

Demand



1,400pcs/m
for coming
months

Production
planning



How many to make?
How much to work?

MPS

Lets make 1,200pcs/m
with overtime!

What model to
make until when?

Resource
planning

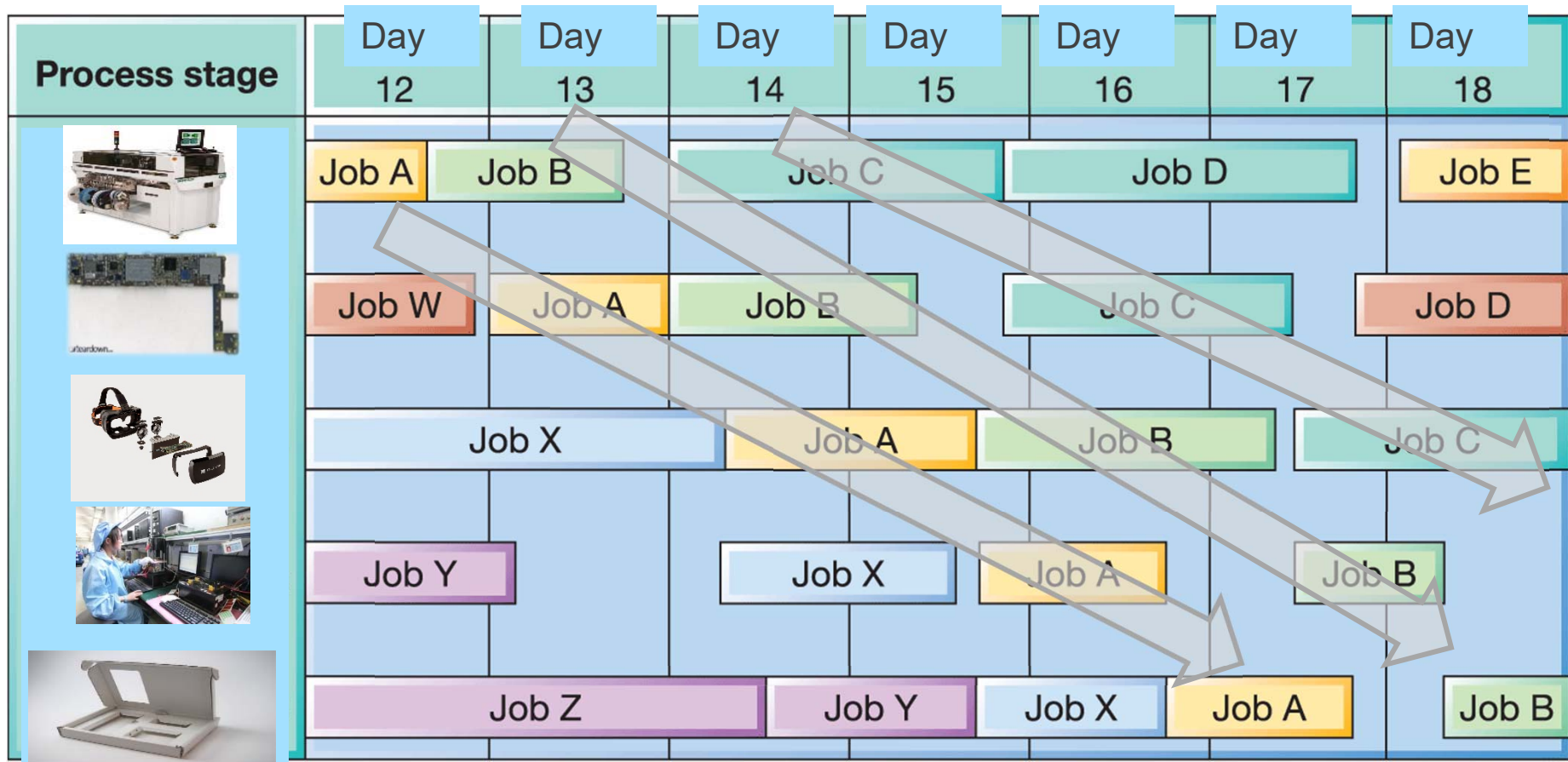


Scheduling

Process stage	Week 12	Week 13	Week 14	Week 15	Week 16	Week 17	Week 18
Initial spec.	Job A	Job B	Job C	Job D	Job E		
Pre-coding	Job W	Job A	Job B	Job C	Job D		
Coding		Job X	Job A	Job B	Job C		
Compat. check	Job Y		Job X	Job A	Job B		
Final test		Job Z	Job Y	Job X	Job A	Job B	

Example of scheduling for line production

Gant Progress chart (note: Job A = Model A)



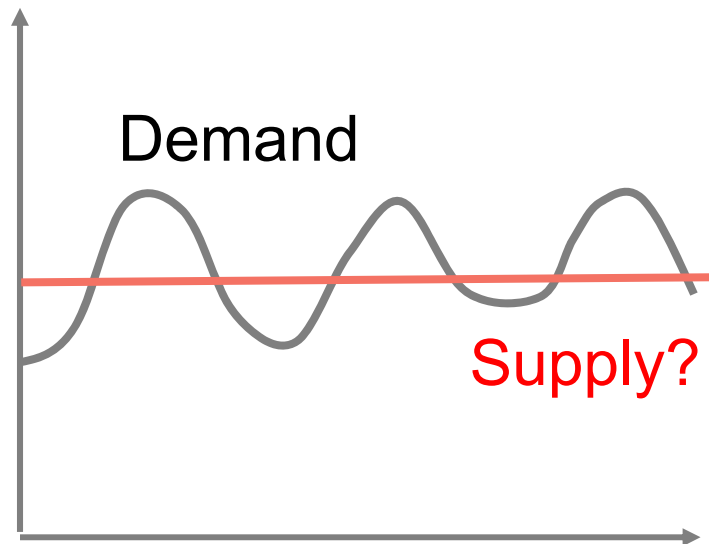


What is operations planning and scheduling?

Operations planning and scheduling is the process of making sure that demand and supply plans are in balance, from aggregate level down to the short-term scheduling level.



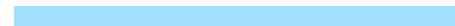
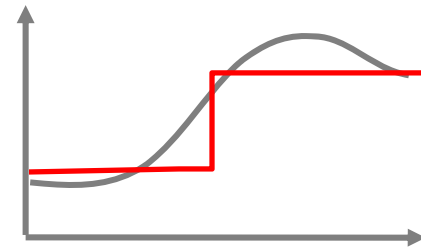
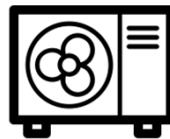
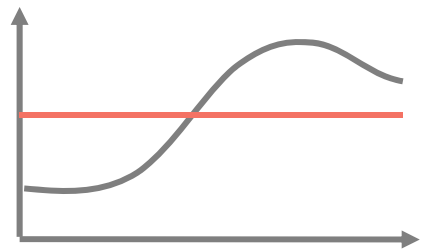
How to cope with mismatch between demand and supply?



- Coping with supply side
- Coping with demand side

Cope with the mismatch from supply side

- Anticipation inventory 
- Workforce adjustment (layoff/hire) 
- Workforce utilization (overtime/undertime) 
- Part-time workers 
- Subcontractors 

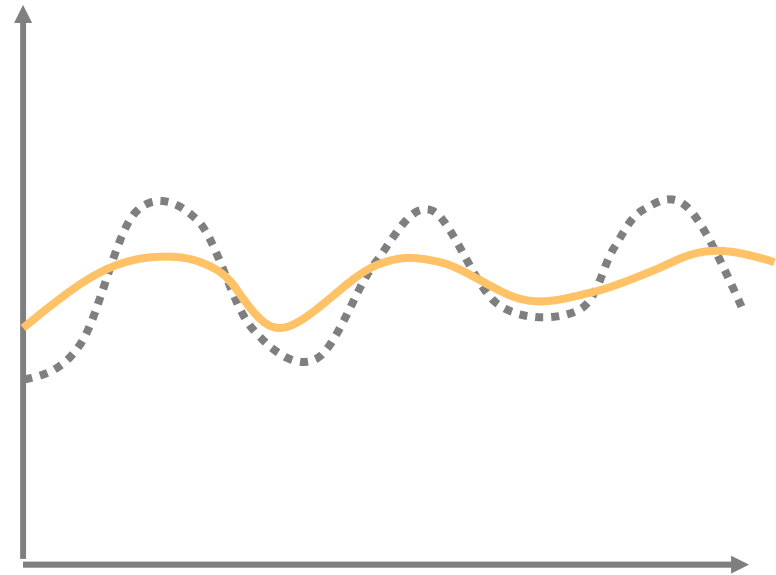


Cope with the mismatch on demand side

Demand management:

Try to change the demand pattern so that the supply side can cope with it easier

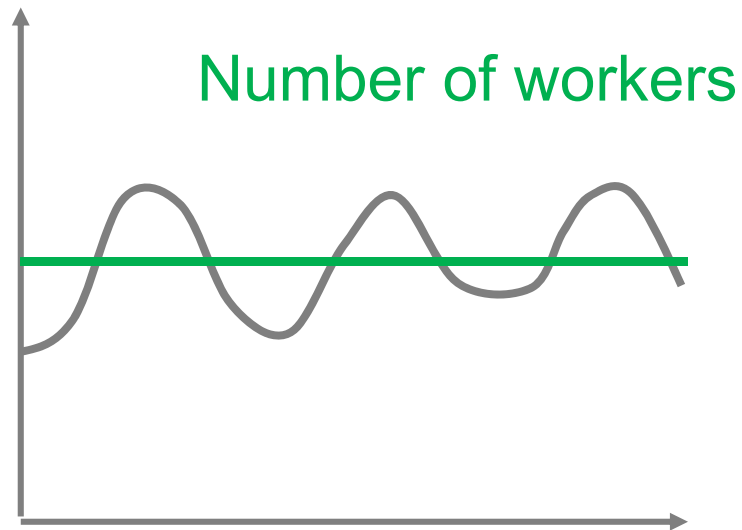
- Promoting pricing
- Reservation
- Complementary products
- Backlogs
- etc.





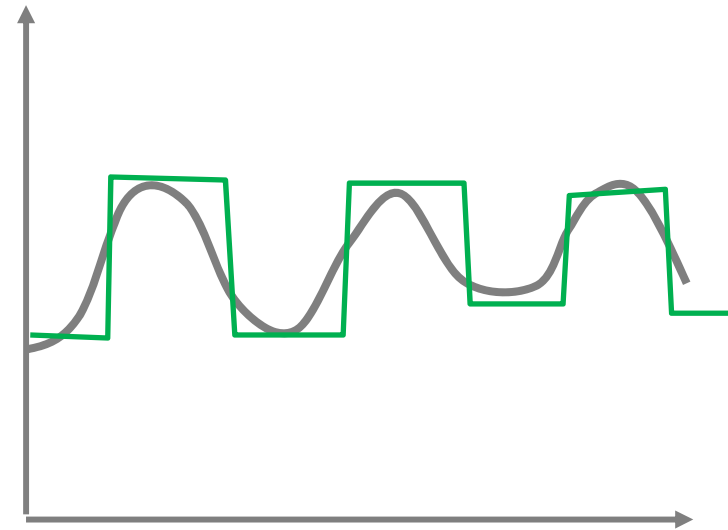
Workforce planning strategies

Level strategy



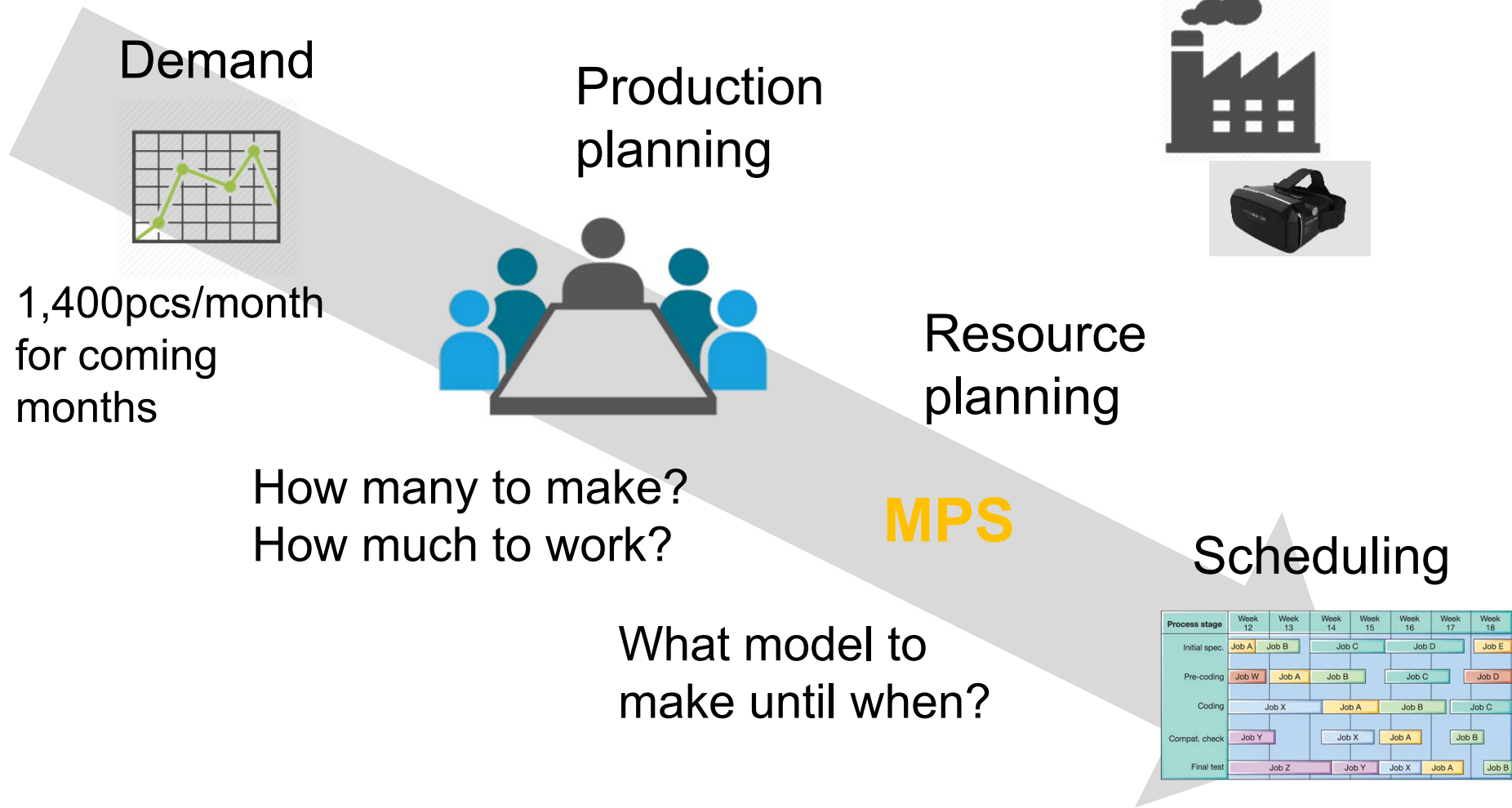
- Overtime cost
- Undertime cost

Chase strategy



- Layoff cost
- Hiring cost

Production planning and scheduling



Production planning

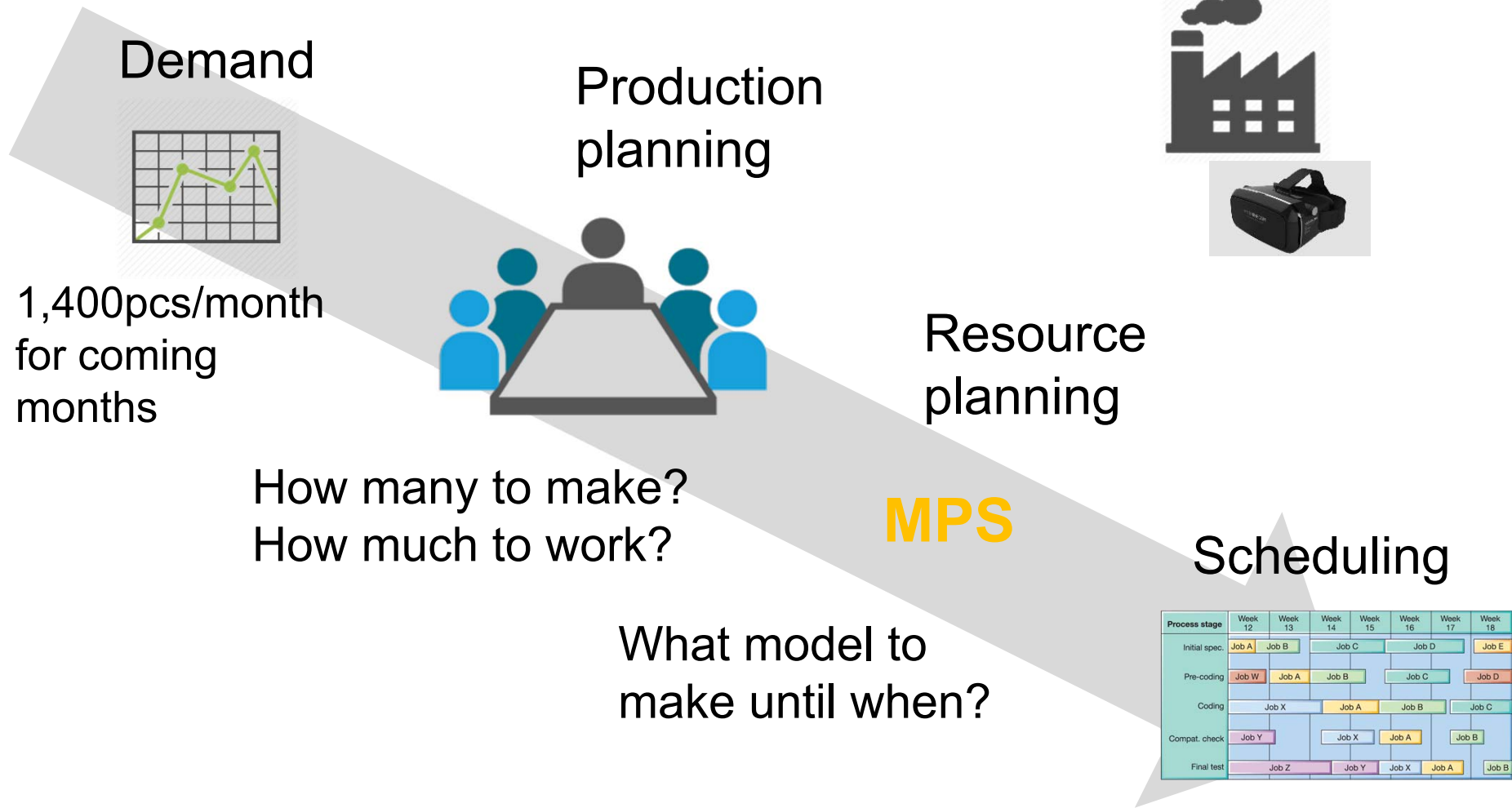
	HISTORY									
	J	F	M	A*	M	J	J	A	S	3 Mos**
SALES										
New forecast	45	55	60	70	85	95	130	110	70	150
Actual sales	52	40	63							
Diff for month	7	-15	3							
Cum		-8	-5							
OPERATIONS										
New Plan	75	75	75	75	75	85	85	85	75	177
Actual	75	78	76							
Diff for month	0	3	1							
Cum		3	4							
INVENTORY										
Plan	85	105	120	125	15	105	60	35	40	198
Actual	92	130	143							

Oct
Nov
Dec



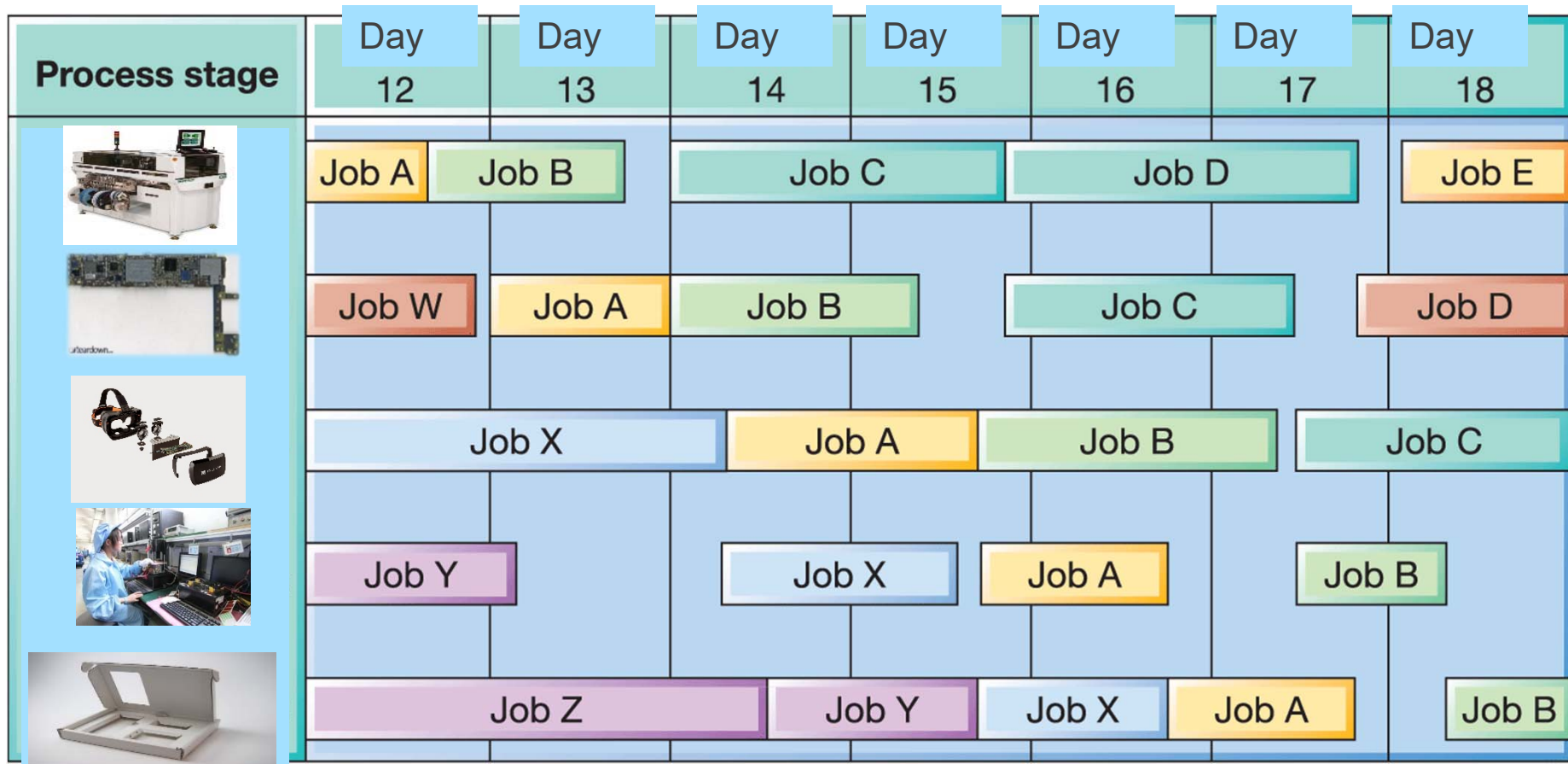
Workforce planning

Production planning and scheduling



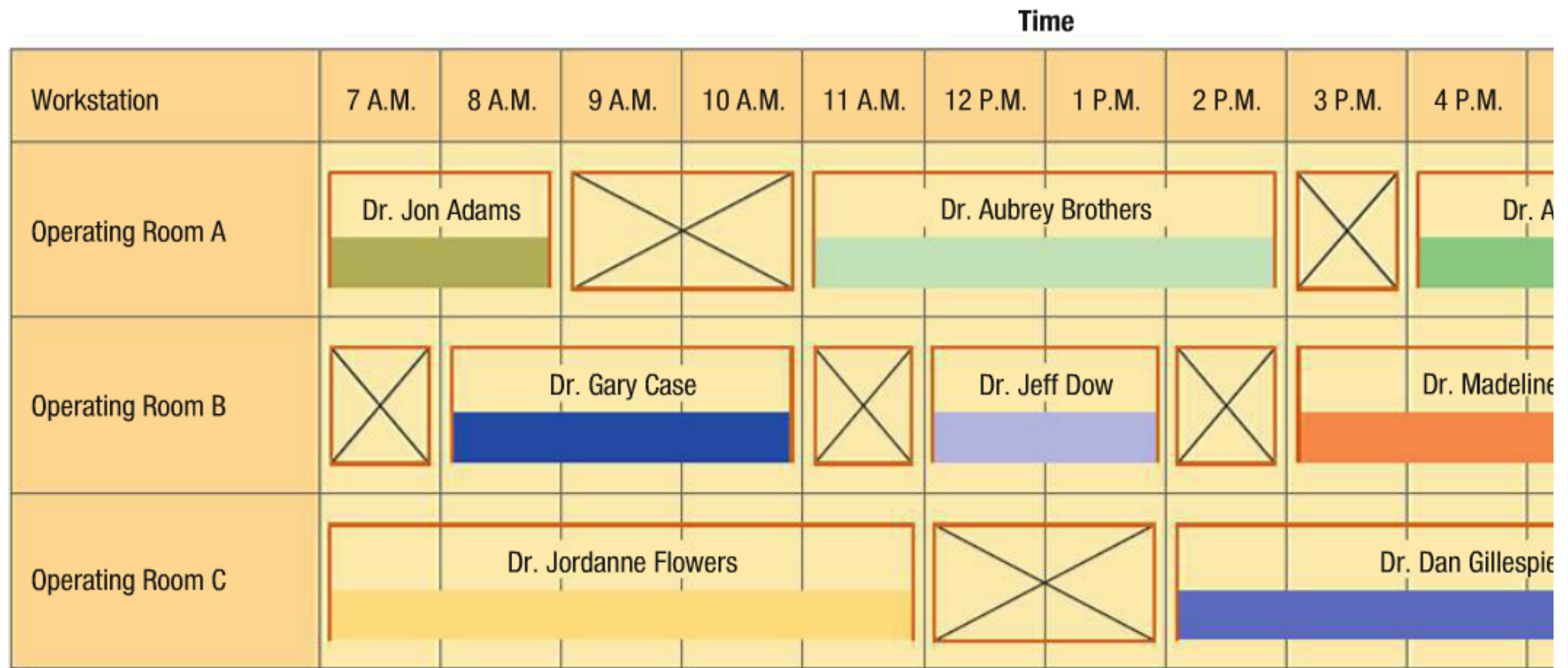
Example of scheduling for line production

Gant Progress chart (note: Job A = Model A)



Example of scheduling for work stations

Gant Workstation chart





Today's topic

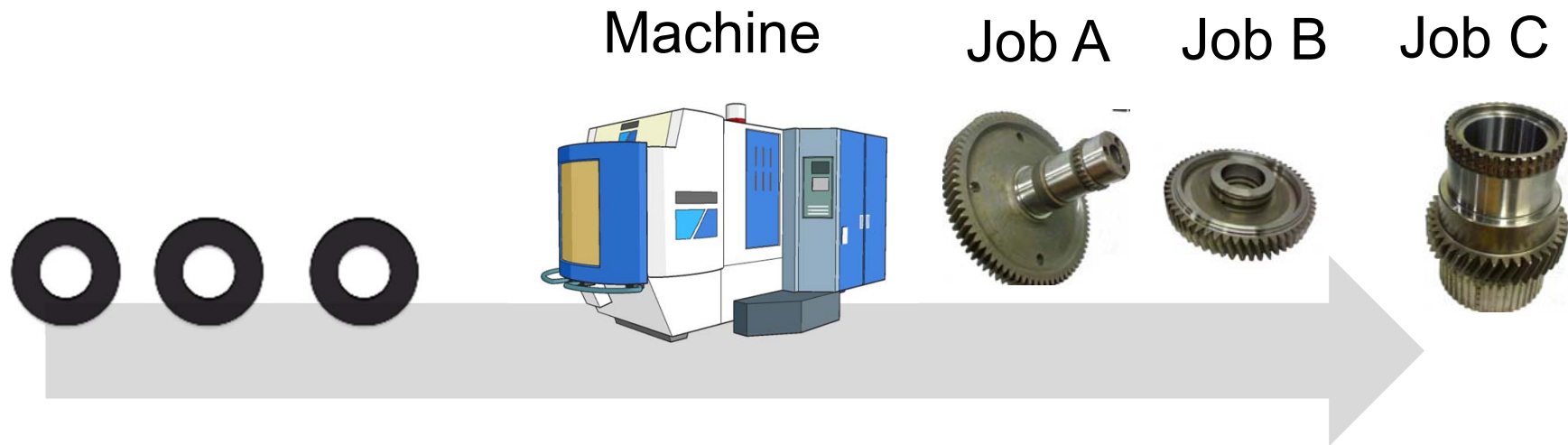
- What is operations planning and scheduling?
- How to cope with mismatch between demand and supply?
- Production planning
- Scheduling
- Job shop scheduling theories



Based on supplemental material

Job shop scheduling problem

- one machine situation

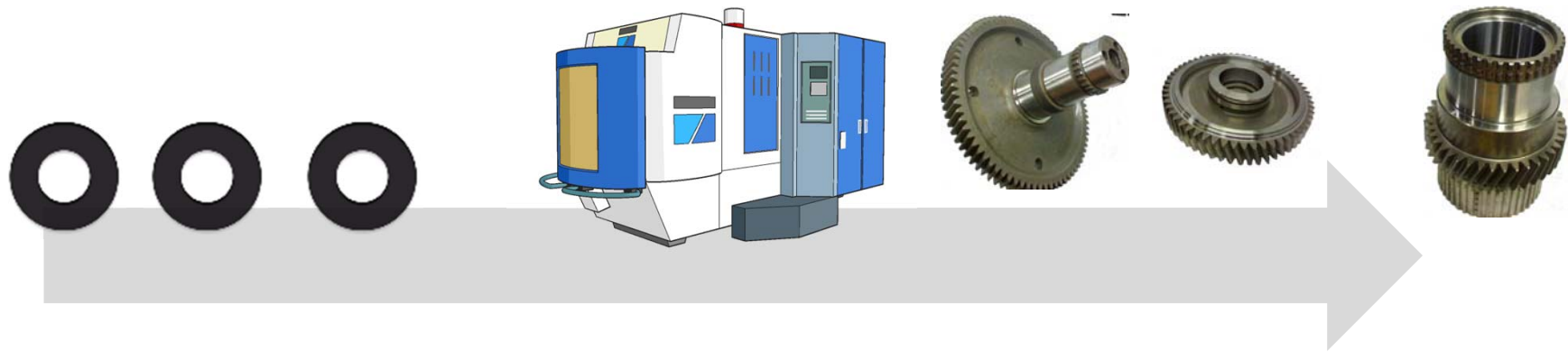


Different job has different
process time and due date...



**In which order
shall we produce?**

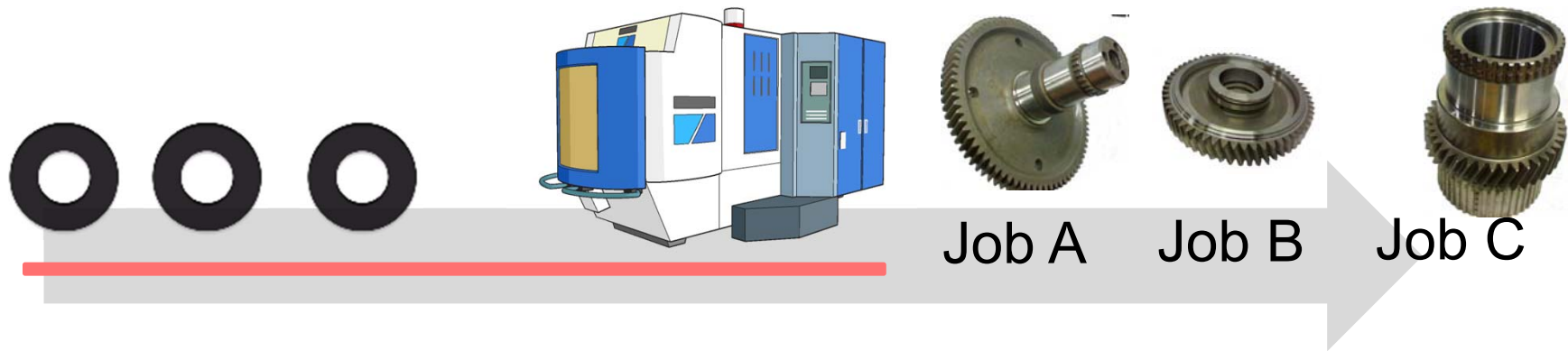
In which order to produce?



Possible objectives:

- Minimize number of delay
- Minimize the largest delay
- Minimize average delay time
- Minimize flow time
- Minimize idle time
- etc.

Terminology



Process time:

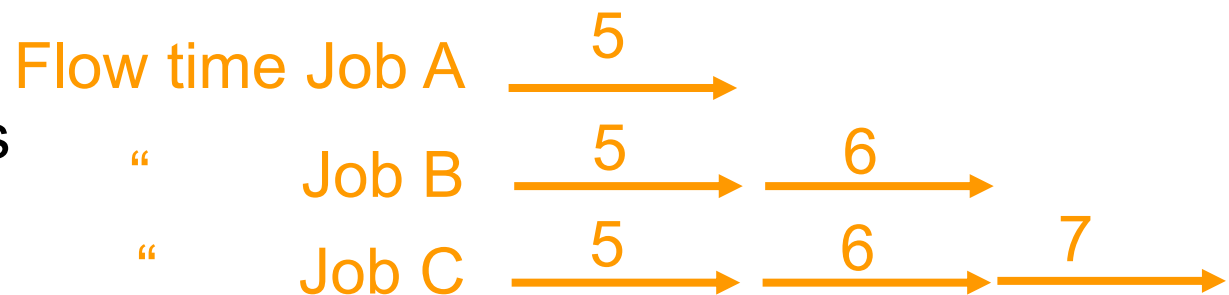
Time a machine takes to do a certain job

5 6 7

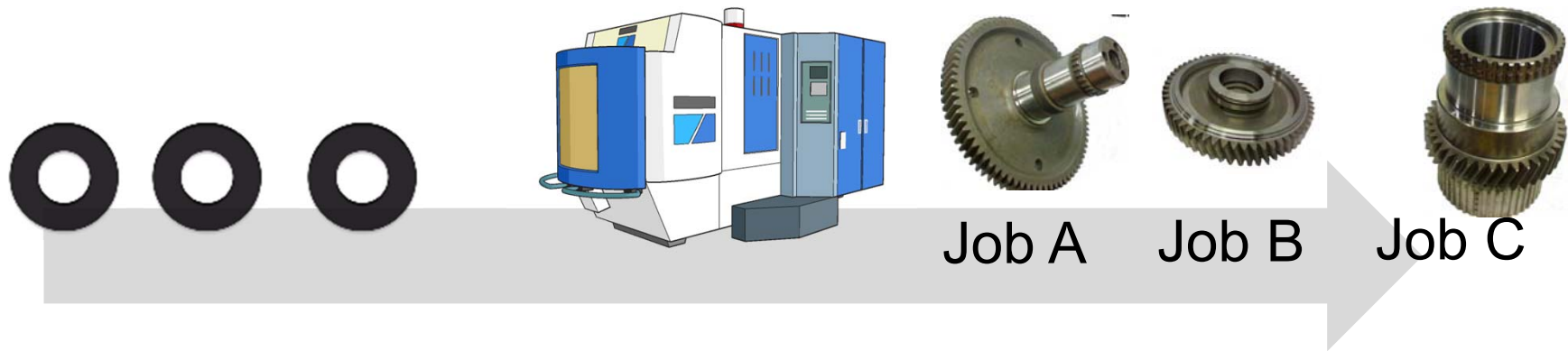
If sequence A - B - C,

Flow time:

Time a job spends in the system



Terminology



Makespan:

Time to complete all jobs

$$5+6+7$$

= Flow time of the last job

Tardiness:

How much the flow time differs (delays) from the due date

Flow time
Job C



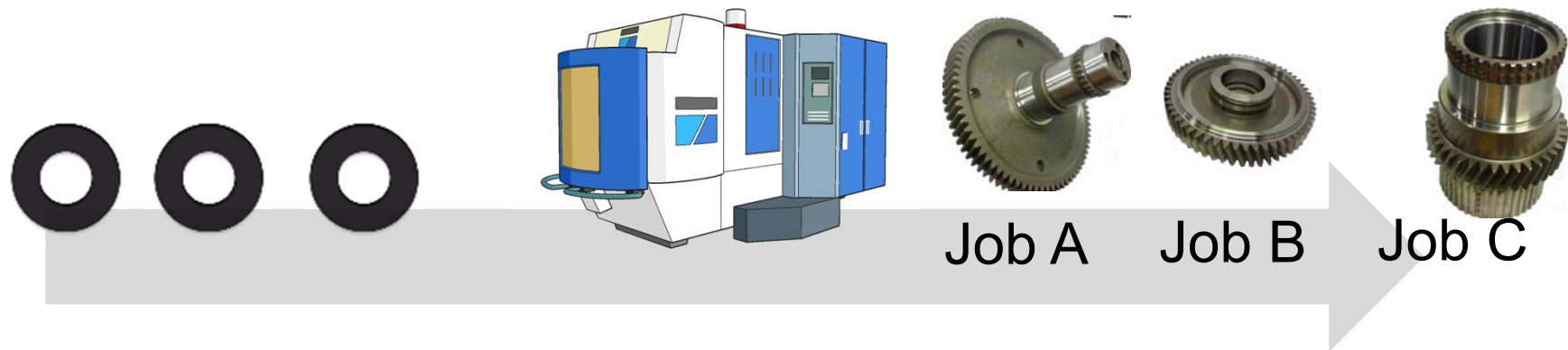
Due date 15

Tardiness

3



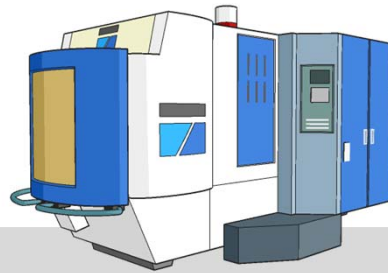
Specific sequencing rules



- FCFS (First-come, First-served)
- SPT (Shortest processing time)
- EDD (Earliest due date)
- CR (Critical ratio)

$$CR = \frac{\text{Due date} - \text{Current time}}{\text{Processing time}}$$

Comparison of sequencing rules



Job 1
Job 2
Job 3
Job 4
Job 5

Example:

<i>Job Number</i>	<i>Processing Time</i>	<i>Due Date</i>
1	11	61
2	29	45
3	31	31
4	1	33
5	2	32

FCFS (First-come First-served)

(Flow time)

<i>Sequence</i>	<i>Completion Time</i>	<i>Due Date</i>	<i>Tardiness</i>
1	11	61	0
2	40	45	0
3	71	31	40
4	72	33	39
5	74	32	42
Totals	268		121

Mean flow time = $268/5 = 53.6$,
Average tardiness = $121/5 = 24.2$,
Number of tardy jobs = 3.

SPT (Shortest Processing time)

Job	Processing Time	Completion Time	Due Date	Tardiness
4	1	1	33	0
5	2	3	32	0
1	11	14	61	0
2	29	43	45	0
3	31	74	31	43
Totals		135		43

Mean flow time = $135/5 = 27.0$,

Average tardiness = $43/5 = 8.6$,

Number of tardy jobs = 1.

EDD (Earliest Due Date)

<i>Job</i>	<i>Processing Time</i>	<i>Completion Time</i>	<i>Due Date</i>	<i>Tardiness</i>
3	31	31	31	0
5	2	33	32	1
4	1	34	33	1
2	29	63	45	18
1	11	74	61	13
Totals		235		33

Mean flow time = $235/5 = 47.0$,

Average tardiness = $33/5 = 6.6$,

Number of tardy jobs = 4.



CR (Critical Ratio)

$$CR = \frac{\text{Due date} - \text{Current time}}{\text{Processing time}}$$

1. On the current time, calculate CR for each job
2. Choose the job that has the smallest CR
3. Erase the job and update the current time
4. Go to step 1

Note: If a certain CR is minus (delayed), chose that job first.
If more than one jobs are minus, chose based on SPT.

Current time: $t = 0$

<i>Job</i>	<i>Processing Time</i>	<i>Due Date</i>	<i>Critical Ratio</i>
1	11	61	61/11 (5.545)
2	29	45	45/29 (1.552)
3	31	31	31/31 (1.000)
4	1	33	33/1 (33.00)
5	2	32	32/2 (16.00)

1st

Current time: $t = 31$

<i>Job</i>	<i>Processing Time</i>	<i>Due Date – Current Time</i>	<i>Critical Ratio</i>
1	11	30	30/11 (2.727)
2	29	14	14/29 (0.483)
4	1	2	2/1 (2.000)
5	2	1	1/2 (0.500)

2nd

Current Time: $t = 60$

<i>Job</i>	<i>Processing Time</i>	<i>Due Date – Current Time</i>	<i>Critical Ratio</i>
1	11	1	1/11 (.0909)
3rd 4	1	-27	-27/1 < 0
4th 5	2	-28	-28/2 < 0

Note: If a certain CR is minus (delayed), chose that job first.
If more than one jobs are minus, chose based on SPT.

CR (Critical Ratio)

Result:

<i>Job</i>	<i>Processing Time</i>	<i>Completion Time</i>	<i>Tardiness</i>
3	31	31	0
2	29	60	15
4	1	61	28
5	2	63	31
1	11	74	13
Totals		289	87

Mean flow time = $289/5 = 57.8$.

Average tardiness = $87/5 = 17.4$.

Number of tardy jobs = 4.

Comparison of sequencing rules - result

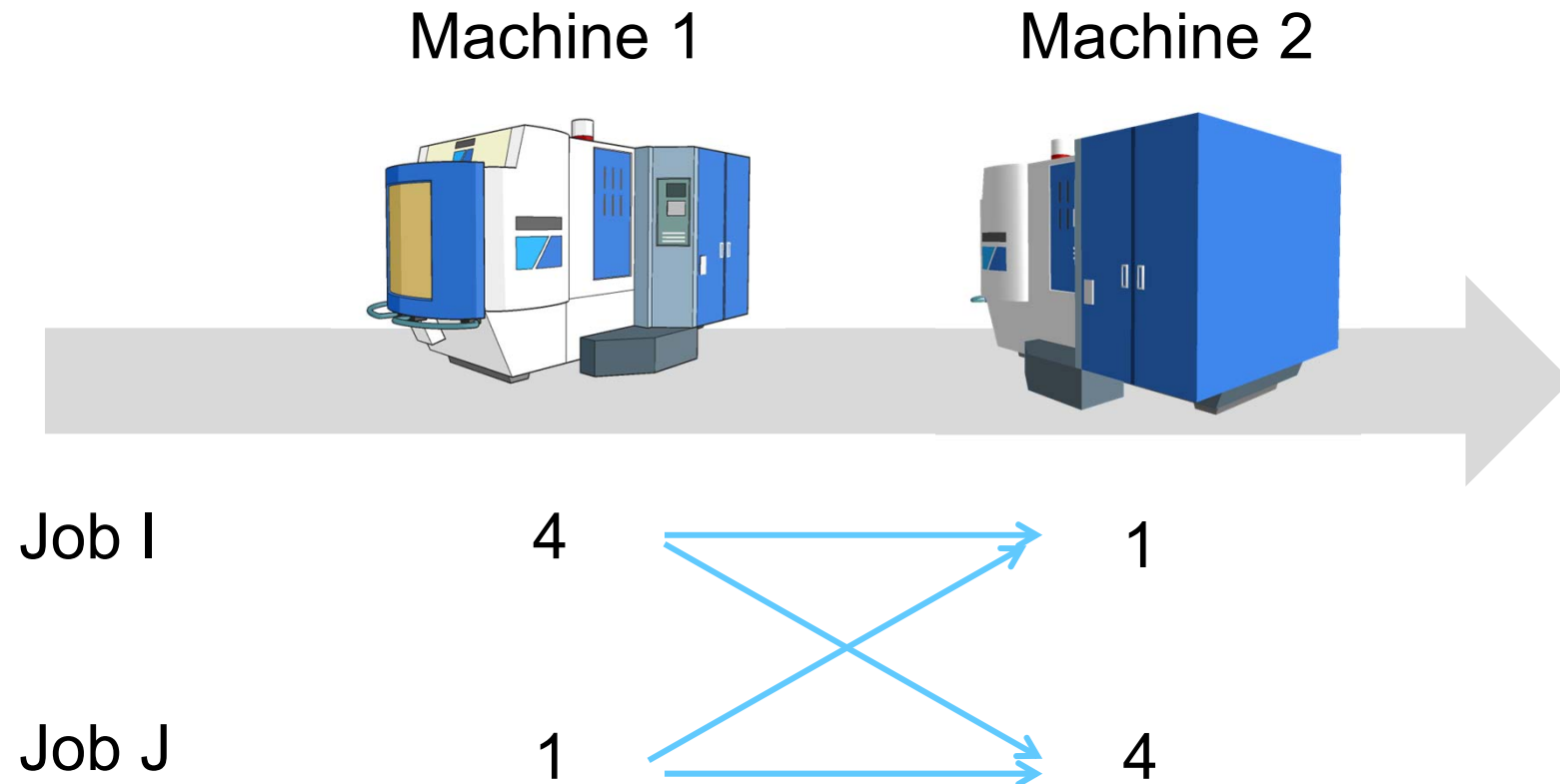
<i>Rule</i>	<i>Mean Flow Time</i>	<i>Average Tardiness</i>	<i>Number of Tardy Jobs</i>
FCFS	53.6	24.2	3
SPT	27.0	8.6	1
EDD	47.0	6.6	4
CR	57.8	17.4	4

Theorem:

- SPT is the rule that minimizes mean flow time
- EDD is the rule that minimizes largest lateness

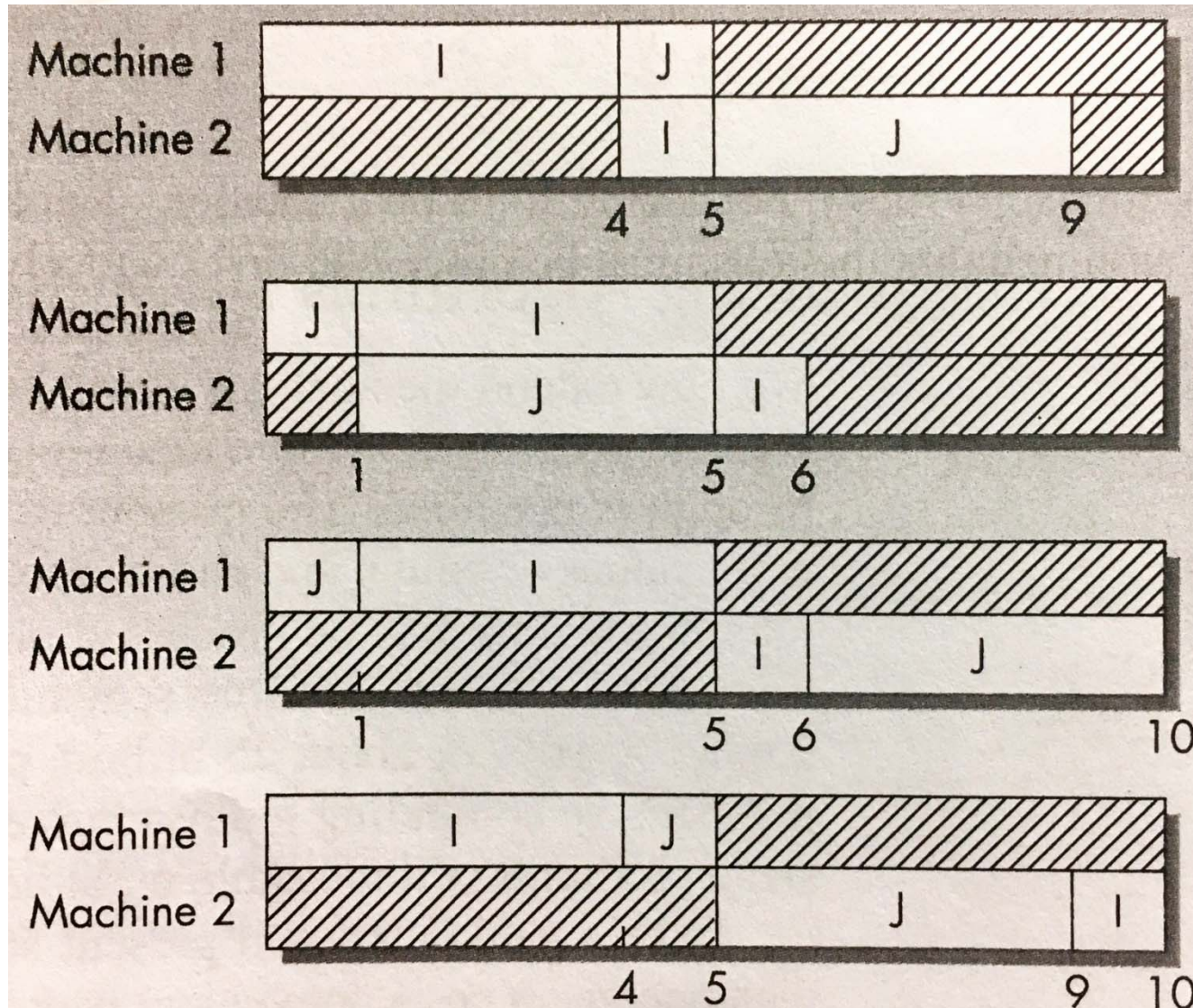
(See the mathematical proofs in the supplement material)

Sequencing algorithm for two machines



Which schedule makes the shortest makespan?

Possible schedules



Permutation
schedule



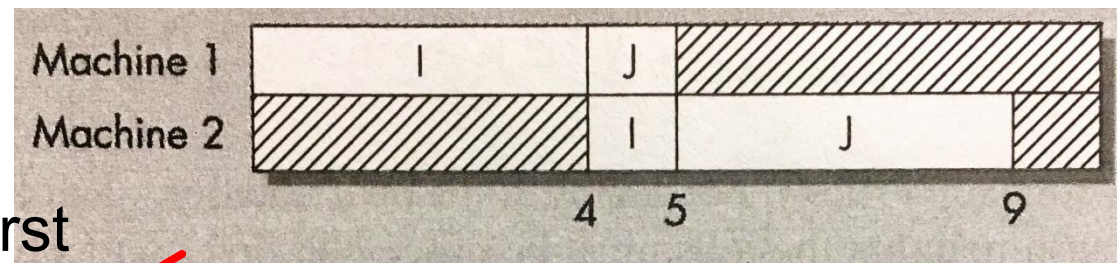
Always
better than
non-
permutation
schedule

Sequencing algorithm for two machines

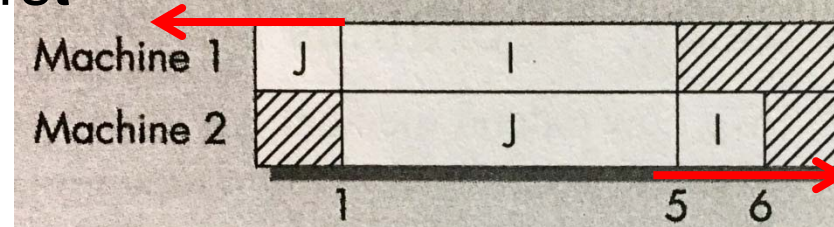
Johnson's rule:

Job i precedes job $i + 1$ if $\min(A_i, B_{i-1}) < \min(A_{i+1}, B_i)$

A_i = Processing time of job i on machine A (or 1)
 B_i = Processing time of job i on machine B (or 2)



Smaller block first
for Machine 1



Smaller block last
for Machine 2

Sequencing algorithm for two machines

Johnson's rule:

Easy way to implement this rule:

1. List the processing time for all jobs for two machines
2. Find the smallest processing time.
3. If it is for the first machine, put it in the first.
If it is for the second machine, put it in the last.
4. Remove the job in the list.
5. Go to 2.

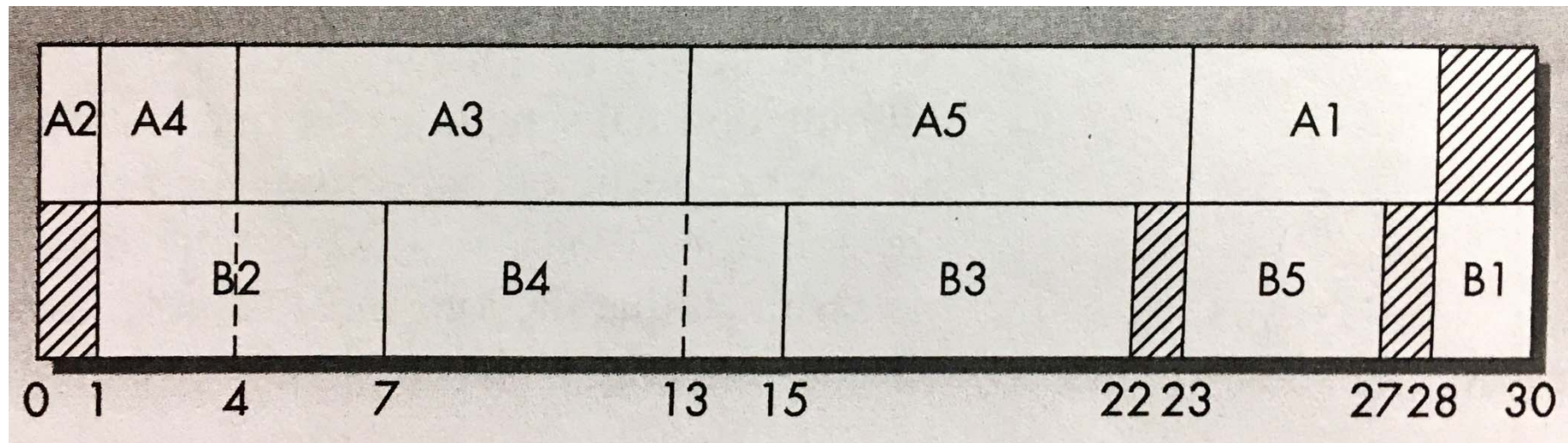
Sequencing algorithm for two machines

Johnson's rule:

<i>Job</i>	<i>Machine A</i>	<i>Machine B</i>
1	5	2
2	1	6
3	9	7
4	3	8
5	10	4

Sequencing algorithm for two machines

Johnson's rule:





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